IOE MODELENTRANCE EXAM 2023 SET +

BEATS ENGINEERING

INSTITUTE OF ENGINEERING

Model Entrance Exam

(Set-4 Solutions)

Instructions:

There are 100 multiple-choice questions, each having four choices of which only one choice is correct.

Section-A (1 marks)

- 1) c 2) b
- 2) b 3) a
- 4) a
- 5) a
- 6) b
- 7) b
- 8) b
- 9) a
- 10) c
- 11) d

12) d

13) c $NaCl \Leftrightarrow Na^+ + Cl^ H_2O \Leftrightarrow H^+ + OH^-$

On passing electricity, Na^+ and H^+ ions move towards cathode. The discharge potential of H^+ ions is less than Na^+ ions. Thus, hydrogen ions get discharged easily and hydrogen is liberated.

- 14) d
- 15) a $n = 3, l = 4 \rightarrow 4f$. In f subshell, there are 7 orbitals and each orbital can accommodate a maximum of two electrons, so maximum no. of electrons in 4f subshell = $7 \times 2 = 14$
- 16) c Density = 1.17g/cc = 1170 g/LMolarity of solution = $\frac{Density in g/L}{Molecular weight} = \frac{1170}{36.5} = 32.05 M$
- 17) d Strong conjugate base has a weakest conjugate acid. Since CH₃COOH is weakest acid among the following, therefore its conjugate base is strong.
- 18) a The atomic number of the given element = 2 + 2 + 6 + 2 + 3 = 15The atomic number of the element present just below the above element = 15 + 18 = 33
- 19) b 4(+1) + 2x + 6(-2) = 0 $2x = 8 \Rightarrow x = 4$
- 20) d $NH_4Cl + NaNO_2 \xrightarrow{heat} NH_4NO_2 + NaCl$
 - $NH_4NO_2 \xrightarrow{\Delta} N_2 + 2H_2O$
- 21) a Clark's method is used to remove the temporary hardness of water, in which bicarbonates of magnesium and calcium are reacted with slaked lime Ca(OH)₂
- 22) d Na₂S and NaCN are decomposed on heating with HNO₃ to form H₂S and HCN in gaseous phase otherwise they will give precipitate with AgNO₃.
 - $\begin{array}{l} NaCN + HNO_3 \rightarrow NaNO_3 + HCN \uparrow \\ Na_2S + 2HNO_3 \rightarrow 2NaNO_3 + H_2S \end{array}$
- 23) b
- 24) b Moment of inertia (I) = Mr^2 [I] = [ML^2] Moment of force (F) = ma[F] = [ML^2T^{-2}]
- 25) d
- 26) d The relation $\vec{F} = m\vec{a}$ can only be deduced from Newton's second law, if mass remains constant with time. If mass depends on time, then, this relation cannot be deduced.
- 27) d The direction of the angular velocity is along the axis of rotation.
- 28) c At the equator, g_e = g Rω² When ω = 0, g_e = g Hence, the value of acceleration due to gravity at the equator remains same.
 29) d When a solid sphere falls in vacuum, no viscous force is acting on the sphere and the sphere falls under gravity, due to which sphere never attains terminal velocity.
- 30) c Mass and volume of the gas will remain same, so density of gas will also remain same.
- 31) b Since the gas is compressed adiabatically, dQ = 0, dW = -150 JFrom first law of thermodynamics, dQ = dU + dWdU = -dW = -(-150) = 150 J
- 32) b Tuning fork of 256 Hz will resonate with fork of frequencies 1×256 , 2×256 , 3×256 , ... i.e., 256, 512, 768, ...

Fork of 738 Hz will not resonate.

- When a glass rod is rubbed with silk cloth then some of the electrons from the glass rod get transferred to the silk cloth and 33) a thus the glass rod gets positive charge and the silk cloth gets negative charge. No new charge is created in the process of rubbing.
- 34) d The deflection in the moving coil galvanometer is:

$$\phi = \left(\frac{NAB}{k}\right)I$$

35) a

 $P = \frac{V^2}{R} \Rightarrow P \propto \frac{1}{R}$ When one bulb will fuse out, resistance of the series combination will be reduced. Hence, illumination will increase. The current will decrease. This is because on inserting an iron core in the solenoid, the magnetic field increases and hence 36) b magnetic flux linked with the solenoid increases. As per Lenz's law, the emf induced in the solenoid will oppose this

increase, which can be achieved by a decrease in current.

37) c

 $\sin C = \frac{1}{\mu}$ 38) d

Since, µ is maximum for violet color, critical angle C is minimum for violet colour.

40) b Impurity increases the conductivity.

41) d
$$\sin^{-1}\left(\frac{5}{x}\right) + \sin^{-1}\left(\frac{12}{13}\right) = \frac{\pi}{2}$$

 $\sin^{-1}\left(\frac{5}{x}\right) = \frac{\pi}{2} - \sin^{-1}\left(\frac{12}{13}\right) = \cos^{-1}\left(\frac{12}{13}\right)$
 $\sin^{-1}\left(\frac{5}{x}\right) = \sin^{-1}\left(\frac{5}{13}\right)$
 $x = 13$
42) d By sine formula,
 $\frac{a}{\sin a} = \frac{b}{\ln a}$
 $\frac{b}{\sin a^{\circ}} = \frac{b}{\sin a}$
 $\sin B = \frac{4}{6} = \frac{2}{3}$
 $B = \sin^{-1}\left(\frac{2}{3}\right) = \sin^{-1} x$
 $x = \frac{2}{3}$
43) a Clearly, $1 + \sin x \ge 0$
 $\therefore \cos x - \sin x = 1$
It is satisfied by $x = 0, x = 2\pi, x = \frac{3\pi}{2}$
Hence, 3 solutions are possible.
44) d $\vec{a} + \vec{b} = \vec{c}$
 $\left|\vec{a} + \vec{b}\right|^{2} = |\vec{c}|^{2}$
 $a^{2} + b^{2} + 2ab \cos \theta = c^{2}$
 $1 + 1 + 2(1)(1) \cos \theta = 1$
 $\cos \theta = -\frac{1}{2}$
 $\theta = \frac{2\pi}{3}$
45) b Sum of roots $= -3$
 $-\left(\frac{2a^{2}}{a+1}\right) = -3$
 $2a + 3 = 3a + 3$
 $a = 0$
 \therefore Product of roots $=\frac{3a+4}{a+1} = 4$
46) a $\sum_{n=0}^{\infty} \frac{x^{2n+1}}{(2n+1)!} = \frac{x}{1!} + \frac{x^{3}}{3!} + \frac{x^{5}}{5!} + \cdots = \frac{e^{x} + e^{-x}}{2} = \sin hx$
47) b $c + e = 2d - c$
 $e - c = 2d - c$
 $= c - c = 2d - c - c = 2d - 2c = 2(d - c)$
48) d $\frac{(1+i)^{2}}{i(2i-1)} = \frac{1+2i+i^{2}}{i(2i-1)} = \frac{1+2i-1}{i(2i-1)} = \frac{2i}{i(2i-1)} = \frac{4i+2}{-5} = -\frac{4}{5}i - \frac{2}{5}$

49) a First we write six '+' signs at alternate places i.e., by leaving one place vacant between two successive '+' signs. Now there are 5 places vacant between these signs and there are two places vacant at the ends. If we write 4 '-' signs at these 7 places then two '-' will come together. Hence, total number of ways = ${}^{7}C_{4} = 35$

Section-B (2 marks)

- 61) b For something to be fundamental, it has to be an essential part of something. In this instance, the fundamental shift means that the rules around shopping have changed significantly; therefore, 'major' is the best option.
- 62) d In the second paragraph we are told that 'Whilst there were concerns about online trading in the early days, this has obviously declined now and as confidence in the internet grows, so too does online shopping.' This helps us to see that people were less confident about buying goods on the internet initially, but their confidence has now grown thus making option D correct. We do not have direct evidence to support any of the other three statements.
- 63) a The second paragraph tells us that people are busy and that they have less time to visit the shops. We are also told that shopping online allows consumers to shop when it suits them hence it is an way to fit more into their busy lives.
- 64) a Option A is false as the first paragraph tells us about the fundamental shift in shopping patterns in the last three years. Option B is true 'a trip to the shops is still regarded by many as an enjoyable past-time'. Options C and D are also true 'consumers can shop when it suits them and can also use price comparison and review websites to ensure they are getting the best deal.

65) b	$N_1 V_1 = N_2 V_2$ (NaOH) (Acid)	
	$\frac{1}{10} \times 25 = N_2 \times 20$	
	$N_2 = 0.125$	
	Strength = Normality \times Eq. mass	
	Eq. mass $=\frac{7.875}{0.125} = 63$	
66) d	$CaCO_3 \xrightarrow{a} CaO + CO_2$	
	Molar mass of $CaCO_3 = 100 \text{ g/mol}$	
	10 g of 90% pure lime = $\frac{10 g}{100 a/mal} \times \frac{90}{100} = 0.09 moles CaCO_3$	
	0.09 moles of $CaCO_3$ on heating gives 0.09 moles of CO_2	
	At STP, 1 mole $CO_2 = 22.4 \text{ L}$	
	At STP. 0.09 mole $CO_2 = 0.09 \times 22.4 = 2.016 L$	
67) c	Millimoles of $CH_3COOH = 0.1 \times$	10 = 1
	Millimoles of $CH_3COONa = 0.1 \times$	20 = 2
	$p_H = p_{ka} + \log \frac{ confugate base }{[acid]} = 4.74 + \log \frac{2}{1} = 4.74 + 0.30 = 5.04$	
68) a	Electronic Configuration	Group
	$[Ne]3s^23p^3$	V
	$[Ne]3s^23p^2$	IV
	$[Ar]3d^{10}4s^24p^3$	V
	$[Ne]3s^23p^1$	
	Since, ionization energy increases in a period and decreases in a group, $[Ne]3s^23p^3$ configuration has the highest	
60) b	10112ation energy among the given elements.	
09)0	stability Hence structure (b) will l	be the most stable carbocation
70) b		
71) d	$\frac{Wt.of \ Oxygen}{Wt.of \ Ag} = \frac{Wt.of \ Ag}{Wt.of \ Ag}$	
	Eq.Wt.of Oxygen Eq.Wt.of Ag 16 Wt of Ag	
	$\frac{1}{8} = \frac{1}{108}$	
	Wt. of Ag deposited = 21.60 gm	
72) c	$3\sin A = 6\sin B = 2\sqrt{3}\sin C = k$	c (say)
	$\frac{\sin A}{1/2} = \frac{\sin B}{1/6} = \frac{\sin C}{1/2\sqrt{2}} = k$	
	$a = \frac{k}{2} b = \frac{k}{2} c = \frac{k}{2}$	
	$u = \frac{1}{3}, b = \frac{1}{6}, c = \frac{1}{2\sqrt{3}}$	
	$\cos A = \frac{b^2 + c^2 - a^2}{2} = \frac{\frac{\kappa}{36} + \frac{\kappa}{12} - \frac{\kappa}{9}}{2} = \frac{1 + 3 - 4}{2} = 0$	
	$2bc$ $2\frac{k^2}{18}$	4
	$A = 90^{\circ}$	
73) b	Putting $x = 1$	2
	Sum of coefficients in the expansion of $(1 - 3x + 10x^2)^n$ is $(1 - 3 + 10)^n = 8^n = a$	
	And sum of coefficients in the expansion of $(1 + x^2)^n$ is $(1 + 1)^n = 2^n = b$: $a = 9^n = (2^n)^3 = b^3$	
74	$\therefore a = 8^n = (2^n)^s = b^s$	
/4) a	By given conditions	Ι.
	a 2ar ar^2 are in A P	
	$a+ar^2$ – 2 –	
	$\frac{1}{2} = 2ar$	
	$1 + r^2 = 4r$	
	$r^2 - 4r + 1 = 0$	
	$r = \frac{1 \pm \sqrt{10}}{2} = 2 \pm \sqrt{3}$	
75) d	$\Delta = 0$	

$$\begin{vmatrix} 3 & k & -2 \\ 1 & k & 3 \\ 2 & 3 & 4 \end{vmatrix} = 0$$

$$(-12k - 6 + 6k) - (-4k + 27 - 4k) = 0$$

$$k = \frac{33}{2}$$

76) b $i + \sqrt{3} = 2\left(\frac{\sqrt{3}}{2} + i, \frac{1}{2}\right) = 2\left(\cos\frac{\pi}{6} + i\sin\frac{\pi}{6}\right)$

77) d f(x) = 2x i.e., y = 2xFor every value of x, there is distinct value of y. So, it is one-to-one function. And, $x = \frac{y}{x}$ But, for every value of y like 3, 5, 7, ..., there is no natural number in the domain set so it is not onto function. Hence, f is one-to-one but not onto. $\lim_{x \to 0} \frac{\tan x - \sin x}{x^3} = \lim_{x \to 0} \frac{\sin x (1 - \cos x)}{x^3 \cos x} = \lim_{x \to 0} \frac{\sin x}{x} \times \frac{1 - \cos x}{x^2} \times \frac{1}{\cos x} = 1 \times \lim_{x \to 0} \frac{1 - \cos x}{x^2} \times \frac{1}{1}$ 78) a $\begin{array}{l}
x \to 0 & x \\
= \lim_{x \to 0} \frac{\sin x}{2x} \\
= \lim_{x \to 0} \frac{\cos x}{2} = \frac{1}{2} \\
x^{y} = e^{x-y}
\end{array}$ [By L's Hospital rule) 79) d Taking log on both sides, $y \log x = x - y$ $y(1 + \log x) = x$ $y = \frac{x}{1 + \log x}$ $\frac{dy}{dx} = \frac{(1+\log x).1-x.\frac{1}{x}}{(1+\log x)^2} = \frac{\log x}{(1+\log x)^2}$ $\int_0^1 \frac{1}{(x^2+1)^{3/2}} dx$ 80) b Put $x = \tan \theta$ For x = 0, $\theta = 0$ $\therefore I = \int_0^{\pi/4} \frac{\sec^2\theta \, d\theta}{\sec^3\theta \, d\theta} = \int_0^{\pi/4} \cos\theta \, d\theta = |\cos\theta|_0^{\pi/4} = \cos 0 - \cos \frac{\pi}{4} = \frac{1}{\sqrt{2}}$ Volume (V) $= \frac{4}{3}\pi r^3$ 81) d $\frac{dV}{dt} = \frac{4}{3}\pi \cdot 3r^2 \cdot \frac{dr}{dt}$ $2 = 4\pi \cdot (12)^2 \cdot \frac{dr}{dt}$ $\frac{dr}{dt} = \frac{1}{288\pi}$ Now, area = $4\pi r^2$ $\frac{dA}{dt} = 4\pi . 2r . \frac{dr}{dt} = 8\pi . 12 . \frac{1}{288\pi} = \frac{1}{3}$ Required area = $\int_0^2 y \, dx = \int_0^2 \frac{x^2}{4} \, dx = \left|\frac{x^3}{12}\right|_0^2 = \frac{2^3}{12} = \frac{2}{3}$ sq. units 82) b Equation of bisector of 1st equation: 83) d $h(x^2 - y^2) = (a - b)xy$ $(x^2 - y^2) = \frac{(a-b)}{h} xy$ --- (1) For 2nd equation of bisector, $h'(x^2 - y^2) = (a' - b') xy$ $(x^2 - y^2) = \frac{(a'-b')}{h'}xy$ --- (2) From (1) and (2), $\frac{h}{h'} = \frac{(a-b)}{(a'-b')}$ $x^2 + y^2 - 2x - 4y + 7 = 0$ 84) d Centre (h, k) = (-g, -f) = (1, 2)The new circle passes through (1, 2) and has same centre. Radius = $\sqrt{(3-1)^2 + (4-2)^2} = \sqrt{8}$ Now, Equation of circle becomes: $(x-1)^2 + (y-2)^2 = (\sqrt{8})^2$ On solving, we get, $x^{2} + y^{2} - 2x - 4y - 3 = 0$ Centre (0, 3) and directrix parallel to x-axis; 85) b So, ellipse has its major axis along y-axis. Major axis = 2b = 12b = 6Eccentricity (e) = 1/2 $\sqrt{1 - \frac{a^2}{b^2}} = \frac{1}{2}$ $1 - \frac{a^2}{b^2} = \frac{1}{4}$

 $\frac{1 - \frac{a^2}{36}}{a^2} = \frac{1}{4}$ $a^2 = 27$ So, equation of ellipse becomes: $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$ $\frac{x^2}{27} + \frac{(y-3)^2}{36} = 1$ 86) c Equation of plane is: 2x - 3y + 6z - 11 = 0 $\vec{n} = 2\hat{\imath} - 3\hat{\jmath} + 6\hat{k}$ Equation of line is: $\hat{b} = \hat{\iota}$ $\sin\theta = \frac{\vec{b}.\vec{n}}{|\vec{b}||\vec{n}|}$ $\sin(\sin^{-1}\lambda) = \frac{(2\hat{\imath}-3\hat{\jmath}+6\hat{k}).(\hat{\imath}+0\hat{\jmath}+0\hat{k})}{\sqrt{(2)^2+(-3)^2+(6)^2}.\sqrt{(1)^2}}$ $\lambda = \frac{2}{\sqrt{49}} = \frac{2}{7}$ 87) a Time taken by body A, $t_1 = 5 s$ Acceleration of body $A = a_1$ Time taken by body B, $t_2 = 5 - 2 = 3 s$ Acceleration of body $B = a_2$ Distance covered by first body in 5th second after its start, $S_5 = u + \frac{a_1}{2}(2t_1 - 1) = 0 + \frac{a_1}{2}(2 \times 5 - 1) = \frac{9}{2}a_1$ Distance covered by the second body in 3rd second after its start, $S_3 = u + \frac{a_2}{2}(2t_2 - 1) = 0 + \frac{a_2}{2}(2 \times 3 - 1) = \frac{5}{2}a_2$ Since, $S_5 = S_3$ or, $\frac{9}{2}a_1 = \frac{5}{2}a_1$ $a_1: a_2 = 5:9$ Here, $u = 15 m s^{-1}$, h = 490 m88) b Time taken by the stone to reach the ground is: $t = \sqrt{\frac{2h}{g}} = \sqrt{\frac{2 \times 490}{9.8}} = 10 \ s$ If m is the mass of the ball, then its total initial energy at height $h = \frac{1}{2}mu^2 + mgh$ 89) c Energy after collision = 50% of $\left(\frac{1}{2}mu^2 + mgh\right) = \frac{1}{2}\left(\frac{1}{2}mu^2 + mgh\right)$ As the ball rebounds to height h, so $\frac{1}{2}\left(\frac{1}{2}mu^2 + mgh\right) = mgh$ or, $\frac{1}{2}mu^2 = \frac{1}{2}mgh$ $u = \sqrt{2gh} = \sqrt{2 \times 9.8 \times 10} = 14 \ m/s$ Here, Surface tension (S) = $2.5 \times 10^{-2} Nm^{-1}$ 90) d $r = 6 mm = 6 \times 10^{-3} m$ $P = 0 mm = 6 \times 10^{-9} m$ Excess pressure inside the soap bubble, $P = \frac{4S}{r} = \frac{4 \times 2.5 \times 10^{-2}}{6 \times 10^{-3}} = 16.7 Pa$ As $V_T = V_0 (1 + \gamma \Delta T)$ $\frac{V_T - V_0}{V_0} = \gamma \Delta T$ $\frac{0.24}{100} = 40 \gamma$ 91) a $\gamma = \frac{0.24}{100 \times 40} = 6 \times 10^{-5} \,^{\circ}C^{-1}$ Coefficient of linear expansion $\alpha = \frac{\gamma}{3} = \frac{6 \times 10^{-5}}{3} = 2 \times 10^{-5} \text{ °C}^{-1}$ Work done in isothermal process is: $W = nRT \ln \frac{v_2}{v_1} = 1 \times 8.31 \times 310 \times \ln \frac{2v_1}{v_1} = 1.786 \times 10^3$ 92) d Amount of heat absorbed = $\frac{1.786 \times 10^3}{4.2}$ cal = 425.4 cal $T_m = 2\pi \sqrt{\frac{l}{g_m}}$ and $T_e = 2\pi \sqrt{\frac{l}{g_e}}$ 93) c $\frac{T_m}{T_e} = \sqrt{\frac{g_e}{g_m}}$

$$T_{m} = \sqrt{\frac{g_{m}}{g_{m}}} \times T_{e} = \sqrt{\frac{g_{m}}{g_{m}}} \times 3.5 = 8.4 \text{ s}$$
94) b The given equation of a wave is:

$$y = 10 \sin\left(\frac{2\pi}{4}t + \alpha\right)$$
At $t = 0, y = 5 \text{ cm}$

$$5 = 10 \sin \alpha$$

$$\frac{1}{2} = \sin \alpha$$

$$\alpha = \frac{\pi}{6}$$
Hence, the total phase at t= 7.5 s is:

$$\phi = \frac{\pi}{a}, \times 7.5 + \alpha = \frac{\pi}{3} + \frac{\pi}{a} = \frac{3\pi}{a} = \frac{\pi}{2}$$
95) a When a charged capaciton of capacitance C₁ is connected in parallel to an uncharged capacitor of capacitance C₂, the charge is shared between them till both attain the common potential which is given by:

$$V' = \frac{g_{1}+g_{2}}{C_{1}+C_{2}} = \frac{G_{1}V}{C_{1}+C_{2}} = \frac{G_{1}V}{C_{1}+C_{2}}$$
96) b In first case, $15 = E + 3r \cdots (2)$
Subtract (2) from (1), we get, $r = \frac{3}{5} \Omega$
From (1),
 $12 = E - 2 \times \frac{3}{4}$

$$E = 12 + \frac{6}{5} = \frac{66}{5}$$
97) c As, $B_{V} = \sqrt{3} B_{H}$
Also, $\tan \delta = \frac{B_{H}}{B_{H}} = \frac{\sqrt{3}B_{H}}{B_{H}} = \sqrt{3}$
 $\delta = \tan^{-1}(\sqrt{3}) = 60^{\circ}$
98) b Current in the circuit, $P = l^{2}R = 5^{2} \times 22 = 550 W$
99) a Here, $u = -40 \text{ cm}, v = +80 \text{ cm}, f = ?$
 $\frac{1}{r} = \frac{1}{60} - \frac{1}{40} = \frac{1}{280} = \frac{1}{400} = \frac{1}{400}$
 $f_{2} = -400 \text{ cm}$
100) a As $eV_{0} = h(v - v_{0})$
 $V_{0} = \frac{h(v - v_{0})}{e} = \frac{663 \times 10^{-34} (02 \times 10^{44} - 33 \times 10^{14})}{16 \times 10^{-19}} = 2 W$

Thank You!!!!!!